

AME40453 - Automation and Controls  
C2 Pre-Lab Assignment

**For the following questions, please express your answers as algebraic equations written on a separate sheet of paper, and show your work. Then, transcribe the equations into your lab notebook.**

1. Write down the governing 1<sup>st</sup> order differential equation for temperature  $T$  with simple proportional feedback controller, where  $\dot{q} = k_p (T_s - T)$ .
2. Using the equation you just wrote, derive an equation for the equilibrium temperature in terms of the system parameters:  $mc_P$ ,  $hA$ ,  $k_p$ , etc. How does it compare to the set-point  $T_s$ ? Will the actual temperature converge to the set-point  $T_s$ ?
3. Using your equation from problem 2, derive an equation for the thermal time constant  $\tau$  in terms of the system parameters:  $m$ ,  $c_P$ ,  $h$ ,  $k_p$ , etc.
4. Sketch the time constant as a function of the proportional gain  $k_p$ .